

1 Given that $n > 0$

make n the subject of the formula $y = \frac{n^2 + d}{n^2}$

$$\begin{aligned}
 y &= \frac{n^2 + d}{n^2} \\
 &\quad \times n^2 \quad \textcircled{1} \\
 yn^2 &= n^2 + d \\
 &\quad - n^2 \quad \textcircled{1} \\
 yn^2 - n^2 &= d \\
 n^2(y-1) &= d \quad \textcircled{1} \\
 &\quad \div (y-1) \\
 n^2 &= \frac{d}{y-1} \\
 &\quad \sqrt{} \quad \textcircled{1} \\
 n &= \sqrt{\frac{d}{y-1}}
 \end{aligned}$$

$$n = \sqrt{\frac{d}{y-1}}$$

(Total for Question 1 is 4 marks)

2 Make x the subject of $y = \frac{5-2x}{x+3}$

$$y = \frac{5-2x}{x+3}$$

$$y(x+3) = 5-2x$$

$$yx + 3y = 5 - 2x \quad (1)$$

$$yx + 2x = 5 - 3y \quad (1)$$

$$x(y+2) = 5-3y \quad (1)$$

$$x = \frac{5-3y}{y+2} \quad (1)$$

$$x = \frac{5-3y}{y+2}$$

(Total for Question 2 is 4 marks)

- 3 (a) Make a the subject of $d = g + 2ac$

$$d = g + 2ac$$

$$d - g = 2ac \quad (1)$$

$$2a = \frac{d - g}{c}$$

$$a = \frac{d - g}{2c} \quad (1)$$

$$a = \frac{d - g}{2c}$$

(2)

(Total for Question 3 is 2 marks)

4 Make x the subject of $y = \sqrt{\frac{x+1}{x-4}}$

$$y = \sqrt{\frac{x+1}{x-4}}$$

$$y^2 = \frac{x+1}{x-4} \quad (1)$$

$$y^2(x-4) = x+1 \quad (1)$$

$$y^2x - 4y^2 = x+1$$

$$y^2x - x = 4y^2 + 1 \quad (1)$$

$$x(y^2 - 1) = 4y^2 + 1$$

$$x = \frac{4y^2 + 1}{y^2 - 1} \quad (1)$$

$$x = \frac{4y^2 + 1}{y^2 - 1}$$

(Total for Question 4 is 4 marks)

5 (b) Make t the subject of the formula $p = at - d$

$$\begin{aligned} p &= at - d \\ p + d &= at \quad (1) \\ t &= \frac{p+d}{a} \quad (1) \end{aligned}$$

$$t = \frac{p+d}{a}$$

(2)

(Total for Question 5 is 2 marks)

- 6 (a) Make c the subject of $A = \frac{c}{y} - 5z$

$$\begin{aligned} A &= \frac{c}{y} - 5z \\ Ay &= c - 5yz \quad \text{①} \\ c &= Ay + 5yz \\ c &= y(A + 5z) \quad \text{①} \end{aligned}$$

$$c = y(A + 5z)$$

(2)

(Total for Question 6 is 2 marks)

7 (b) Make c the subject of the formula $p = \sqrt{\frac{ac+8}{3+c}}$

$$p = \sqrt{\frac{ac+8}{3+c}}$$

$$p^2 = \frac{ac+8}{3+c} \quad (1)$$

$$p^2(3+c) = ac+8$$

$$3p^2 + p^2c = ac+8 \quad (1)$$

$$3p^2 - 8 = ac - p^2c \quad (1)$$

$$3p^2 - 8 = c(a - p^2)$$

$$c = \frac{3p^2 - 8}{a - p^2} \quad (1)$$

$$\frac{3p^2 - 8}{a - p^2}$$

(4)

(Total for Question 7 is 4 marks)

8 (b) Make c the subject of $g = \frac{c+3}{4+c} - 7$

$$g+7 = \frac{c+3}{4+c} \quad (1)$$

$$(g+7)(4+c) = c+3$$

$$4g + 9c + 28 + 7c = c + 3 \quad (1)$$

$$9c + 7c - c = 3 - 28 - 4g \quad (1)$$

$$c(g+6) = -4g - 25$$

$$c = \frac{-(4g+25)}{g+6} \quad (1)$$

$$c = \frac{-(4g+25)}{g+6}$$

(4)

(Total for Question 8 is 4 marks)

9 $a = \frac{14}{3x-7} \quad x = \frac{7}{4y-3}$

Express a in the form $\frac{py+q}{ry+s}$ where p, q, r and s are integers.

Give your answer in its simplest form.

$$a = \frac{14}{3\left(\frac{7}{4y-3}\right)-7} \quad (1)$$

$$= \frac{14}{\frac{21}{4y-3} - 7}$$

$$= \frac{14(4y-3)}{21 - 7(4y-3)} \quad (1)$$

$$= \frac{56y - 42}{21 - 28y + 21}$$

$$= \frac{56y - 42}{42 - 28y}$$

$$= \frac{14(4y-3)}{14(3-2y)} \quad (1)$$

$$a = \frac{4y-3}{3-2y}$$

(Total for Question 9 is 3 marks)

10 Make t the subject of $n^2 = \frac{4d+t^3}{t^3}$

$$n^2 t^3 = 4d + t^3 \quad (1)$$

$$n^2 t^3 - t^3 = 4d$$

$$t^3 (n^2 - 1) = 4d \quad (1)$$

$$t^3 = \frac{4d}{n^2 - 1} \quad (1)$$

$$t = \sqrt[3]{\frac{4d}{n^2 - 1}} \quad (1)$$

$$t = \sqrt[3]{\frac{4d}{n^2 - 1}}$$

(Total for Question 10 is 4 marks)

11 (d) Make t the subject of $c = t^3 - 8v$

$$t^3 = c + 8v \quad (1)$$

$$t = \sqrt[3]{c + 8v} \quad (1)$$

$$t = \sqrt[3]{c + 8v}$$

(2)

(Total for Question 11 is 2 marks)

12 Make x the subject of $y = \sqrt[3]{\frac{6+5x}{x+4}}$

$$y^3 = \frac{6+5x}{x+4} \quad (1)$$

$$y^3 x + 4y^3 = 6 + 5x \quad (1)$$

$$y^3 x - 5x = 6 - 4y^3 \quad (1)$$

$$x(y^3 - 5) = 6 - 4y^3$$

$$x = \frac{6 - 4y^3}{y^3 - 5} \quad (1)$$

$$x = \frac{6 - 4y^3}{y^3 - 5}$$

(Total for Question 12 is 4 marks)

13 (b) Make e the subject of $w = \sqrt{\frac{e+g}{ef-d}}$

$$w^2 = \frac{e+g}{ef-d} \quad (1)$$

$$w^2(ef-d) = e+g$$

$$w^2ef - w^2d = e+g \quad (1)$$

$$w^2ef - e = g + w^2d \quad (1)$$

$$e(w^2f - 1) = g + w^2d$$

$$e = \frac{g + w^2d}{w^2f - 1} \quad (1)$$

$$e = \frac{g + w^2d}{w^2f - 1}$$

(4)

(Total for Question 13 is 4 marks)